



### Introduction to ONETEP

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# **Outline**



- Density matrix reformulation of DFT
- Localised function representation of density matrix
- Linear-scaling with localised functions
- Linear-scaling with large basis set accuracy
	- NGWFs, density kernel
	- Plane waves and psinc basis set
	- FFT box
	- Parallel scaling
- Compilation and hardware requirements
- Running a simple calculation
- Functionality available
- Examples of ONETEP applications

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### Density Functional Theory (DFT)

$$
E[n] = \sum_{i} \int \psi_{i}^{*}(\mathbf{r}) \left( -\frac{1}{2} \nabla^{2} \right) \psi_{i}(\mathbf{r}) d\mathbf{r} + E_{\text{ext}}[n] + E_{\text{Coul}}[n] + E_{xc}[n]
$$

$$
\underbrace{\int V_{ext}(\mathbf{r}) n(\mathbf{r}) d\mathbf{r}}_{\mathbf{r}} \underbrace{\left( \frac{1}{2} \int \int \frac{n(\mathbf{r}) n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r} d\mathbf{r}' \right)}
$$

A hierarchy of approximations for *Exc*[*n*] are available ("Jacob's ladder")

- Local density approximation (LDA): e.g. VWN or CAPZ correlation
- Generalised Gradient Approximations (GGA): e.g. BLYP, PW91, PBE
- Meta-GGAs: e.g. B95,B98,ISM,KCIS,PKZB,TPSS,VSXC
- Hybrid (including exact exchange): e.g. B3LYP, B1PW91, B1LYP, B1B95, mPW1PW91, PBE1PBE







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## DFT simulations





### Computational bottlenecks in DFT





### Computational cost of DFT: cubic-scaling



- Not suitable for biomolecules/nanostructures with **thousands of atoms**
- A **linear-scaling reformulation of DFT** is needed



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# Linear-scaling DFT

• Physical principle

#### **Nearsightedness of electronic matter** W. Kohn, *Phys. Rev. Lett*. **76**, 3168 (1996)

• Linear-scaling approaches

• Practical implementation

In molecules with non-zero band gap, the density matrix decays exponentially  $\rho(\mathbf{r}, \mathbf{r}') \sim e^{-\gamma |\mathbf{r} - \mathbf{r}'|} \to 0 \text{ as } |\mathbf{r} - \mathbf{r}'| \to \infty$ 

Truncate exponential "tail"  $\rho(\mathbf{r}, \mathbf{r}') = 0$  when  $|\mathbf{r} - \mathbf{r}'| > r_{\text{cut}}$ 

- Localised orbitals
- No diagonalisation
- Energy minimisation
- Sparse matrices and algorithms  $- O(N)$ memory and CPU cost





### Density matrix DFT: energy expression

DFT energy with molecular orbitals

$$
E_{\text{DFT}} = \sum_{i} f_i \int \psi_i^*(\mathbf{r}) \left( -\frac{1}{2} \nabla^2 \right) \psi_i(\mathbf{r}) d\mathbf{r} + \int V_{ext}(\mathbf{r}) n(\mathbf{r}) d\mathbf{r} + \frac{1}{2} \int \int \frac{n(\mathbf{r}) n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r} d\mathbf{r}' + E_{xc}[n]
$$

Density matrix

$$
\rho(\mathbf{r}, \mathbf{r}') = \sum_{n} f_n \psi_n(\mathbf{r}) \psi_n^*(\mathbf{r}') = \sum_{\alpha, \beta} \phi_\alpha(\mathbf{r}) K^{\alpha \beta} \phi_\beta^*(\mathbf{r}')
$$

**Density** 

 $n(\mathbf{r}) = \rho(\mathbf{r}, \mathbf{r})$ 

Molecular orbitals

Localised orbitals

DFT energy with density matrix

$$
E_{\rm DFT}=-\sum_{\alpha,\beta}K^{\alpha\beta}\int\phi_{\beta}^{*}(\mathbf{r})\frac{1}{2}\nabla^{2}\phi_{\alpha}(\mathbf{r})d\mathbf{r}+\int V_{\rm ext}(\mathbf{r})n(\mathbf{r})d\mathbf{r}+\frac{1}{2}\int\int\frac{n(\mathbf{r})n(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|}d\mathbf{r}d\mathbf{r}'+E_{xc}[n]
$$



# Conflicting requirements Linear-scaling DFT in practice



How can we have linear-scaling cost with "cubic-scaling accuracy" ?



## The ONETEP linear-scaling approach

- Use a minimal number of  $\{\phi_\alpha\}$
- Optimise both **K** and  $\{\phi_{\alpha}\}\$
- Aim is to have linear-scaling DFT with large basis set accuracy



$$
\rho(\mathbf{r}, \mathbf{r}') = \sum_{\alpha\beta} \phi_{\alpha}(\mathbf{r}) K^{\alpha\beta} \phi_{\beta}(\mathbf{r}')
$$
  
Non-orthogonal  
Generalised  
Wannier Functions  
(NGWFs)

- NGWFs confined to spherical regions
- Density kernel **K** sparse by truncation

C.-K. Skylaris, A. A. Mostofi, P. D. Haynes, O. Dieguez, M. C. Payne, *Phys. Rev. B* **66**, 035119 (2002).

C.-K. Skylaris, P. D. Haynes, A. A. Mostofi and M. C. Payne, *J. Chem. Phys.* **122**, 084119 (2005).

C.-K. Skylaris, P. D. Haynes, A. A. Mostofi and M. C. Payne, *Phys. Stat. Sol. (b)* **243**, 973 (2006).



### Linear-scaling with near-complete basis set accuracy



Example: binding energy calculation

#### ONETEP linear-scaling DFT



#### Cubic-scaling DFT



P. D. Haynes, C.-K. Skylaris, A. A. Mostofi and M. C. Payne, *Chem. Phys. Lett.* **422** 345 (2006).



C.-K. Skylaris, O. Dieguez, P. D. Haynes and M. C. Payne, *Phys. Rev. B* **66**, 073103 (2002).

### Psinc basis set

- •Real linear combinations of plane waves
- •Highly localised
- •Orthogonal

$$
\phi_{\alpha}(\mathbf{r}) = \sum_{i \in \text{LR}_{\alpha}} D_i(\mathbf{r}) \, C_{i,\alpha}
$$



$$
D_j(\mathbf{r}) = \frac{1}{N} \sum_{\mathbf{G}}^{\mathbf{G} \cdot (\mathbf{r} - \mathbf{r}_j)} e^{i \mathbf{G} \cdot (\mathbf{r} - \mathbf{r}_j)}
$$



• A. A. Mostofi, P. D. Haynes, C.-K. Skylaris and M. C. Payne, *J. Chem. Phys.* **119**, 8842 (2003) • D. Baye and P. H. Heenen, *J. Phys. A: Math. Gen*. **19**, 2041 (1986)



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Distance from nucleus

### Pseudopotentials

- Replace the strong Coulomb nuclear potential V by a much weaker *pseudopotential*  $V_{ps}$  which mimics the effect of the core electrons
- Only keep the valence electrons, in smooth valence wave functions  $\Psi_{\text{ps}}$  without oscillations in the core region
- Eliminating the 1/r singularity at the nucleus and the rapid oscillations of the valence wavefunctions near it make it possible to use a plane wave basis set and converge with a reasonable kinetic energy cut-off
- Even hydrogen atoms (obviously, no core electrons) have pseudopotentials in plane wave calculations!
- Beyond the core radius  $r_c$ , the  $V_{ps}$  and  $\Psi_{ps}$  match the all-electron calculation
- Determining r<sub>c</sub>, as well as which electrons to remove as "core" and which to keep as "valence" is an art and requires experience
- Small  $r_c$  leads to "hard" pseudopotentials which are more transferable but require more plane waves (higher  $E_{max}$ ) and therefore more computational effort
- There are several recipes for generating pseudopotentials and libraries of these are publicly available, see for example<http://opium.sourceforge.net/> and [http://www.sas.upenn.edu/rappegroup/research/pseudo-potential](http://www.sas.upenn.edu/rappegroup/research/pseudo-potential-gga.html)[gga.html](http://www.sas.upenn.edu/rappegroup/research/pseudo-potential-gga.html)
- Before selecting a pseudopotential it is crucial to test it thoroughly, ideally against all-electron calculations



### Energy optimisation in ONETEP







### Psinc basis energy cut-off





# FFT box technique



## FFT box technique



### FFT box

C.-K. Skylaris, A. A. Mostofi, P. D. Haynes, C. J. Pickard & M. C. Payne, *Comp. Phys. Comm.* **140**, 315 (2001) A. A. Mostofi, C.-K. Skylaris, P. D. Haynes & M. C. Payne, *Comp. Phys. Comm.* **147**, 788 (2002)



### Linear-scaling with the number of atoms *Example: ONETEP calculations on amyloid fibril proteins*



*J. T. Berryman, S. E. Radford and S. A. Harris, Biophysical Journal, 97 1 (2009)*

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### Linear-scaling with the number of atoms

Example: ONETEP calculations on graphite segments

Calculations run on 160 2.0 GHz Intel Skylake cores (4 nodes, with 2x20 cores per node) with 192 GB per node



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# Compiling ONETEP

Simple multi-platform build system, needs:

- Fortran 2003/2008 compiler
- BLAS and LAPACK (or SCALAPACK) numerical libraries
- FFT library: vendor-supplied or FFTw
	- www.fftw.org
- MPI library for parallel version
- OpenMP



# Running ONETEP

- Parallel computer
	- Minimum 1 GB per processor (core)
	- Typically distribute 10-100 atoms per processor
	- Cross-over >100 atoms
- Prepare input file: free format
	- Documentation at [www.onetep.org](http://www.onetep.org/)
- Supply pseudopotential files (**.recpot** format)
- We suggest that instead of running ONETEP directly, you run the **onetep\_launcher** script which sets up correctly the runtime environment and does important checks



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# Input file

- Keywords of different types:
	- Integer
	- Boolean
	- String
	- Real
	- Physical (real + unit)
	- Block data e.g. atomic positions, delimited by **%block** and **%endblock**
- Atomic units by default (hartree and bohr)



! Example input file for the ONETEP program ! Formaldehyde molecule

cutoff energy 600 eV

%block lattice cart 48.00 0.00 0.00 0.00 48.00 0.00 0.00 0.00 48.00 %endblock lattice cart

#### %block positions\_abs



#### %block species



#### %block species\_pot

- O oxygen.recpot
- C carbon.recpot
- H hydrogen.recpot

%endblock species\_pot





# ONETEP calculation outline

- Initialisation phase:
	- Construct initial NGWFs (STOs or PAOs)
	- Construct initial charge density (atomic superposition) and effective potential
	- Construct initial Hamiltonian
	- Obtain initial density kernel using iterative approach



# ONETEP calculation outline continued

- Main optimisation phase:
	- Combination of nested self-consistent loops
	- Outer loop optimises the NGWFs (density kernel fixed)
	- Inner loop optimises the density kernel (NGWFs fixed) using Density Matrix Minimisation approaches



##### ###### ####### ####### Linear-Scaling Ab Initio Total Energy Program Release for academic collaborators of ODG Version 7.3.2 Remote: https://github.com/cksdaddy/onetep cks.git Local branch: master Commit ID: b4c6aa44c0d7f1571eb406a78225d0ff2140eea1 Date: Fri Aug 23 10:21:36 2024 +0100 Working tree clean Authors: Jacek Dziedzic, Peter D. Haynes, Nicholas D. M. Hine, Arash A. Mostofi, Mike C. Payne and Chris-Kriton Skylaris Contributors: J. Aarons, L. Andrinopoulos, P. W. Avraam, R. A. Bell, A. Bhandari, G. A. Bramley, R. J. Charlton, S. J. Clark, R. J. Clements, G. C. Constantinescu, F. Corsetti, N. Corsini, O. Dieguez, S. M. M. Dubois, K. K. B. Duff, J. M. Escartin, M. Escobar Azor, A. Greco, H. Helal, Q. O. Hill, L. P. Lee, J.-H. Li, T. Li, E. B. Linscott, G. Moynihan, D. D. O`Regan, O. K. Okan, E. Parkinson, M. J. S. Phipps, C. J. Pickard, J. C. A. Prentice, M. I. J. Probert, L. E. Ratcliff, M. Robinson, A. Ruiz Serrano, M. dos Santos Dias, J. S. Spencer, E. W. Tait, G. Teobaldi, D. Turban, V. Vitale, K. A. Wilkinson, C. Weber, J. C. Womack, Chengcheng Xiao, N. Yeung, and T. J. Zuehlsdorff.

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• Parallel strategy, calculation parameters

```
Job started: 28-08-2024 16:49 (+0100)
Reading parameters from file "h2co 2-threads.dat" ...... done
If your calculation crashes here, before "Checking processes and threads..."
is displayed, then your stack size is insufficient.
If so, use "ulimit -s unlimited" at runtime.
You can disable this check with "check stack size F".
Checking processes and threads...
      Default threads: 2
   Running with 2 MPI processes.
   There are 2 MPI processes running on the same node as the root process.
   Each MPI process is using:
                                                                               Input file parameters for 
               2 threads for simulation cell FFTs.
                                                                                OMP threads
               2 threads for threaded FFT box operations.
                                                                                threads_max 2
               2 threads for loops over batched FFT box operations.
                                                                                threads_per_fftbox 2 
               2 threads in other parallel regions.
  MPI Interface: S1 (use mpi f08) (-DMPI -DUSE MPI F08).
                                                                                threads_num_fftboxes 2
   MPI ASYNC PROTECTS NONBLOCKING: Yes. MPI SUBARRAYS SUPPORTED: Yes.
                                                                                threads per cellfft 2
   FFTW Interface: OMP-capable and MODERN. (-DUSE MODERN FFTW specified).
   GPU Interface: None.
   GPU FFT Backend: None.
\ldots done
Basic input checks...... done
Reading geometry and species blocks from file "h2co 2-threads.dat" ...
 <species_atomic_set> block not found: NGWF initialisation set to SOLVE
\ldots done
                        ---------- INPUT FILE ----------
```




• Simulation cell, FFT box, grid spacing



• NGWF initialisation to pseudo-atomic orbitals (PAOs)

```
Atom SCF Calculation for 0 : Z (AE atom) = 8 : Z (PS atom) = 6
Config String:
Orbitals (num,occ): 2 2.00 4.00
Orbitals (num, 1): 2 0 1
Atom SCF converged after 33 iterations to a total energy of -15.71589674
Atom SCF Calculation for C : Z (AE atom) = 6 : Z (PS atom) = 4
Config String:
Orbitals (num,occ): 2 2.00 2.00
Orbitals (num,1): 2 0 1
Atom SCF converged after 33 iterations to a total energy of -5.33577996
Atom SCF Calculation for H : Z (AE atom) = 1: Z (PS atom) = 1
Config String:
Orbitals (num, occ): 1 1.00
Orbitals (num, 1): 1 0
Atom SCF converged after 30 iterations to a total energy of -0.43623914NGWF initialisation ...... done
```


• Initialise and refine density kernel

```
Density kernel initialisation
Writing density kernel to file "h2co 2-threads.dkn" ... done
>>> Optimising kernel for current NGWFs:
   iter |
                energy (Eh)
                                    \vert rms gradient \vertdE (Eh)
                                                       commutator
             -2.230601586111E+015.3808E-02
    \mathbf{1}4.4840E-02
    \mathcal{P}-2.233073648394F+013.8281F - 023.1901F - 02-2.4721E-023
             -2.235530086009E+011.1889E-02
                                                       9,9074E-03
                                                                     -2.4564E - 024
             -2.235864046835E+016.8691E - 035.7242E-03
                                                                     -3.3396E - 035
             -2.235945547230F+013.9727F - 033.3106F-03
                                                                     -8.1500F - 04Finished density kernel iterations (5)
```
Writing density kernel to file "h2co 2-threads.dkn" ... done

>>> Density kernel optimised for the current NGWF basis:







########################### NGWF CG iteration 004 ############################# ##



>>> Checking for convergence of NGWFs:

• End of SCF calculation

. . . . . . . . . . . . . \*\*\* NGWF optimisation converged \*\*\* RMS NGWF gradient  $=$ 0.00000126859037 Criteria satisfied: -> RMS NGWF gradient lower than set threshold. 



#### <<<<< CALCULATION SUMMARY >>>>>





 $=$  $=$  $=$  $=$  $=$ 

Total energies

- Different exchange-correlation functionals:
	- LDA (Ceperley-Alder-Perdew-Zunger, Vosko-Wilk-Nusair, PW92)
	- GGA (PW91, PBE, revPBE, RPBE, BLYP, XLYP, WC)
	- Non-local exchange-correlation functionals for dispersion (e.g. Langreth and Lundqvist, VV10)
	- Meta-GGAs, e.g. PKZB, B97m-v
	- Hartree-Fock exchange and hybrid functionals, B3LYP, PBE0
- Spin polarisation
- DFT+D (empirical dispersion)
- DFT+U
- Charge-constrained DFT
- Finite temperature DFT for metallic systems (Ensemble DFT, AQUA-FOE)
- Embedding (e.g. mGGA in LDA), using EMFT
- DFTB (GFN0 available, GFN1 and GFN2 to follow)

Excited states

- Conduction NGWFs
- LR-TDDFT
- LR-TDDFT with the Tamm-Dancoff approximation (TDA)

Boundary conditions and embedding

- Periodic boundary conditions
- Open boundary conditions (Cut-off Coulomb, Martyna-Tuckerman or real-space open boundaries)
- Solvent and electrolyte models
- Electrostatic embedding

Core electrons

- Norm conserving pseudopotentials
- Projector Augmented wave (PAW) approach (all electron)



### Atomic forces and stresses

- Geometry optimisation
- Transition state search
- *Ab initio* molecular dynamics
- Simulation cell relaxation
- Visualisation
	- NGWFs
	- Molecular Orbitals
	- Density and potentials
	- Electron Localisation Function (ELF)

Atomic orbital basis set option

• Instead of NGWFs construct and use SZ, SZP, DZ, DZP, etc atomic orbital basis sets



### Electronic properties

- Density of states (DOS), local DOS, projected DOS
- Atomic charges (Mulliken, IH, Density derived electrostatic and chemical (DDEC) )
- Dipoles and higher moments
- Optimisation of separate NGWF set for accurate conduction bands and optical absorption spectra
- Natural Bond Orbital (NBO) analysis
- Energy Decomposition Analysis (EDA)
- Electron transport
- Distributed multipole analysis

Interface to ASE

GPU port under development

### Simulations in electrolyte and voltage to predict degradation mechanisms in Li-ion batteries



#### *J. Mater. Chem. A* **10** 11426 (2022) *2D Mater*. **8** 015016 (2020)

#### 2-D heterostructures with "exotic" electronic and mechanical properties





ONETEP was required as the cell necessary to keep the strain low for a misaligned heterostructure is very large.

### Drug design from quantum mechanical calculations on entire proteins



#### Motivation for full QM:

- Captures more physics (Polarization, Charge transfer Many-body effects)
- Low empiricism
- Transferable

### *Phys. Chem. Chem. Phys*. **23** 9381 (2021)

Designing new Pd carbide nanoparticle catalysts for selective hydrogenation of acetylene



#### *RSC Advances* **14** 27799 (2024)

#### Organic photovoltaics: Linear-scaling Time-Dependent DFT (LS-TDDFT) calculations of excited states

Colour prediction from excited state calculations: Including the full crystalline environment to predict experiment



#### *J. Phys. Chem. C* **122** 17024 (2018)

### For more information: www.onetep.org





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